## C. U. SHAH UNIVERSITY, WADHWAN CITY.

## Faculty of: Sciences \& Life Sciences

Course: Bachelor of Science (Mathematics)
Semester: I
Subject Code: MAM202-1C
Subject Name:Linear Algebra \& Complex Analysis


## Course Objective :

The main objectives of this course are

- The definitions of matrix and types of matrices.
- Algebra of matrices.
- Methods to solve system of linear equations.
- Eigen value and Eigen vectors of matrices.


## COURSE CONTENTS

## Course Outline for Theory

| UNIT | COURSE CONTENT | TEACHING HOURS |
| :---: | :---: | :---: |
| I | Introduction to Determinants and Matrices, different types of Matrices, theorems on matrices, elementary operations on matrices, Row Echelon \& Reduced Row Echelon form of a Matrix, Solution of system of linear equations, solving system of linear equations simultaneously, Inverse of Matrix, Rank of Matrix, Matrix inversion using RRE form. Characteristic equation of a matrix and Cayley-Hamilton theorem and its use in finding inverse of matrix, Eigen value and Eigen vector of square matrices, eigenvalue of special type of matrices, Diagonalization of matrix. | 15 |
| II | Complex numbers, Polar form of complex number. De'Moivre's theorem, nth roots of a complex number, Fundamental theorem of algebra (statement only), Multiple roots and test for multiplicity. | 15 |
| III | Expansions of $\cos n \theta, \sin n \theta, \tan n \theta$ in terms of $\cos \theta, \sin \theta, \tan \theta$ respectively ( $n \in N$ ). Expansion of $\cos ^{n} \theta, \sin ^{n} \theta$ in a series of cosines or sines of multiple angles of $\theta(n \in N)$. Expansion of $\cos \theta, \sin \theta, \tan \theta$ in terms of $\theta$. Exponential, circular and hyperbolic functions. | 15 |


| SR. <br> NO | COURSE CONTENT | Lab Hours |
| :---: | :--- | :---: |
| $\mathbf{1}$ | RE and RRE form and rank of a matrix, Inverse of a matrix |  |
| $\mathbf{2}$ | Problems based on eigen values and eigen vectors and Diagonalization |  |
| $\mathbf{3}$ | Cayley- Hamilton's Theorem and its applications. |  |
| $\mathbf{4}$ | Descarte's rule of sign, Relation between roots and coefficients. |  |
| $\mathbf{5}$ | Solution of cubic equations (Cardan's method), Solution of biquadratic equations <br> (Ferarri's method) | 30 |
| $\mathbf{6}$ | Algebra of Complex numbers, De'Moivre's theorem. |  |
| $\mathbf{7}$ | Expansions of $\cos n \theta, \sin n \theta, \tan n \theta$ in terms of $\cos \theta, \sin \theta, \tan \theta$ respectively <br> $(n \in N)$. |  |
| $\mathbf{8}$ | Expansion of $\cos ^{n} \theta, \sin ^{n} \theta$ in a series of $\operatorname{cosines}$ or $\operatorname{sines}$ of multiple angles of <br> $\theta(n \in N)$. |  |

## TEACHING METHODOLOGY:

Conventional method (classroom blackboard teaching)
ICT Techniques
Teaching through the classroom
Variety of learning styles and tools (PowerPoint presentations, audio-visual resources, e-resources, seminars, workshops, models)

## LEARNING OUTCOME:

After the successful completion of the course, students will be able to

- Solve systems of linear equations.
- Manipulate matrix algebra and determinants.
- Evaluate Eigen values and Eigen vectors.
- Understand the concepts of complex numbers and some complex functions.

Arrangement of lectures duration and practical session as per defined credit numbers:

| Units | Lecture Duration <br> (In Hrs.) |  | Calculation of <br> Credits <br> (In Numbers) |  | Total <br> Lecture <br> Duration | Credit <br> Calculation |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Theory | Practical | Theory | Practical | Theory+ <br> Practical | Theory+ <br> Practical |
| Unit $\mathbf{- 1}$ | 15 | 30 | 3 | 1 | $45+30$ | 4 |
| Unit $-\mathbf{2}$ | 15 | 30 | 3 | 1 | 4 |  |
| Unit $-\mathbf{3}$ | 15 |  | $\mathbf{3 0}$ | $\mathbf{3}$ | $\mathbf{1}$ | $\mathbf{7 5}$ |
| TOTAL | $\mathbf{4 5}$ | $\mathbf{3 0}$ | $\mathbf{4}$ |  |  |  |

Evaluation:

| Theory Marks | Practical Marks | Total Marks |
| :---: | :---: | :---: |
| 75 | 25 | $\mathbf{1 0 0}$ |

## REFERENCE BOOKS:

1. Advanced Engineering Mathematics', E. Kreyszig, New Age International Publishing Co.
2. 'Complex Variables and Applications', R. V. Churchill, J. W. Brown, McGraw-Hill Book Co.
3. Elementary Linear Algebra', Howard Anton and Chris Rorres, Wiley Pub.
4. A Textbook of Matrices', Shanti Narayan and P. K. Mittal, S. Chand and Co. New Delhi.
5. 'Higher Engineering Mathematics, Thirty-fifth edition', B. S. Grewal, Khanna Publication.
